

## MULTIDIMENSIONAL SMOOTHING USING HYPERBOLIC INTERPOLATORY WAVELETS \*

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**Abstract.** We propose the application of hyperbolic interpolatory wavelets for large-scale  $d$ -dimensional data fitting. In particular, we show how wavelets can be used as a highly efficient tool for multidimensional smoothing. The grid underlying these wavelets is a sparse grid. The hyperbolic interpolatory wavelet space of level  $j$  uses  $O(j^{d-1}2^j)$  basis functions and it is shown that under sufficient smoothness an approximation error of order  $O\left(\binom{j+d-1}{d-1}2^{-2j}\right)$  can be achieved. The implementation uses the fast wavelet transform and an efficient indexing method to access the wavelet coefficients. A practical example demonstrates the efficiency of the approach.

**Key words.** sparse grids, predictive modelling, wavelets, smoothing, data mining.

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